

## A Study on Scope, Applications, Current Challenges and Possible Solutions in the Field of Calculus

*1.Mr. Gorekh Prasad Nayak 2.Soubhagini Mohapatra*  
*Nalanda Institute of Technology, Bhubaneswar*  
*Dept. of Basic Science & Humanities*  
*E-mail ID: gorekhprasad@thenalanda.com*  
*SoubhaginiMohapatra@thenalanda.onmicrosoft.com*

### ABSTRACT

Calculus primarily serves to assist us in tracking changes in quantity over time. The areas between and beneath the curves must be taken into account in the new calculation in addition to the instantaneous change rates and curve slopes that were necessary in the previous calculation. Calculations can be performed in two different ways: independently and integrally. Differential measurement uses the characteristics of trends of change, which include a change in qualities. For integration zones, integral calculus is extremely helpful. The use of calculus in numerous academic disciplines has enhanced the subject of mathematics. "Calculus composed of stones" refers to both the tiny stones and the computation itself.

Keyword: Calculus in Education, Calculus Uses, and Calculus Research and Development are other related terms.

### INTRODUCTION

Although it has mostly been utilised in academics for a long time, calculus is no longer used exclusively in academics. Calculus is the topic that a mathematics degree programme revolves on. There is a lot of study into the computational interpretation of the assessment, and as a result, the subject of evaluation is a very important concept. An analysis of numerous past studies also shown that those in higher education showed negligibly little knowledge of many of the essential concepts of calculus. there has been a lot of disagreement on whether computational logic should be presented to young children, given the number of types of quantitative literacy is difficult for them to grasp (Cipra; Steen; White). the traditional college calculus curriculum emphasises teaching and preparing students with a more extensive variety of calculus content, a system of arranging that knowledge, and a long-term plan of preparing them (Ferrini-Mundy 628). When Romberg and Tufte state that how kids see mathematics is that it is a formal collection of abilities to master all at once, they believe that students perceive mathematics in this manner.

Initiatives to enhance how calculus is taught have arisen because students use many approaches, including simple calculations, to do the analysis and assessment that go into the discipline. Graphic design for most people, the bigger the worry, the rarer it is. The difficult process of learning calculus has resulted in the development of a desire to revise how calculus is taught. As the relevance of calculus in science has been more recognised, emphasis has shifted to whether or not teaching calculators should be included in the curriculum.

### CALCULUS HISTORY

Mathematics ideas that have started off with Theano, the ancient Greek, and William of Ockham, the mediaeval Christian monk, have all played vital roles in developing new ideas. Archimedes used the pendulum form to determine the parabola's area.

Although numerous ideas have been proposed before, it was previously believed that they were not the norm. The computations of volume and region are included in the papyrus. It doesn't get into the details of how they did it.

The Greeks used the exhaustion method, which predicts the idea of the limit, and Archimedes further established the basic measuring techniques crucial to integral measurement.

First coined by an Italian scientist called Cavalieri in the 16th century, the notion of volume was popularised by Evangelista Torricelli in the 17th century. After this first discovery, the Chinese mathematician Zu Gengzhi went on to build on the concept. Alhacen has developed a possible solution for the sum of the fourth power. He used the formulae for the volume of the paraboloid and the fourth power to measure the volume.

At the beginning of the 14th century, Indian mathematicians ran upon an issue that had yet to be solved. Madhava has said that he will hold reciprocal ground. Taylorism, which encompasses a complete political theory, is known in the West as a "kit."

Despite their claims, however, they were unable to demonstrate that calculus was a problem-solving methodology that incorporated various notions from the derivative and the integral.

### **The Modernization of Calculus**

The discovery of calculus is considered the first step in contemporary mathematics. This book gives the reader the best plausible understanding of what has happened in mathematics over the last two thousand years.

### **Von Neumann's Computer**

Cavalieri's theorem postulated that the masses and regions might be thought of as a collection of cross-sections that were all tiny but random. The ideals laid down in this pact were similar to Cavalieri's concepts in *The Process*, but it was not until after World War I that they were rediscovered.

The data supplied by Cavalieri's method may not have been completely valid, and the infinitesimal number it produced is unknown.

It was the comprehensive study of the equations that led to the development of infinitesimals for Cavalieri and the discovery of finite differences. The idea of "equality" might be applied to the infinitely thin, which is made up of a limited number of layers, as long as a certain condition was met. Secondly, in addition to Charles Sanders Peirce, John Wallis, Isaac Barrow, and James Gregory discovered the second basic theorem of calculus.

Isaac Newton used algebra in developing his theory of gravity.

Newton included several rules of substance and chain law as well as other ideas in order to solve mathematical issues. Although Newton presented his ideas on gravity using approximations, he was not aware that the calculations he employed were based on infinitesimals.

With his findings in the 1687 publication of his *Mathematical Principles of Natural Philosophy*, he answered a wide range of topics including celestial motion, the Earth's crust, the motion of a rolling weight, and other aspects of his *Principia Mathematica*. It was apparent from his previous work that he held the principles of Taylor's series close to his heart. He was not consistent with his results, and so his research techniques have been called into question.

### **GOTTFRIED WILHELM LEIBNIZ WAS ANOTHER PERSON WHO CONTRIBUTED TO THE DISCOVERY OF THE FIRST EQUATION.**

Gottfried Wilhelm Leibniz is also credited with the introduction of infinitesimals and also established the notion of individual observation of the calculus. To provide another example, the following functions contain the correct symbol of the differential and integral function of a single variable: As previously noted in the article, Newton was completely confused with his own metaphors and too concerned with the definitions.

In addition, Leibniz also spoke of the measurement, as well as of Newton who built on calculation.

Newton used the physics calculus and Leibniz began the practise of using a different notation for the calculus. Additionally, differential equations, second and higher derivatives, and the idea of approximation polynomials all figured in the research. After finding out about the fundamental theorem of calculus, Newton used the newly discovered knowledge.

Several mathematicians engaged in a heated discussion about who was more directly connected to the discoveries of Newton and Leibniz. It was written down for the first time at the feet of Newton's *Nova Methodus pro Maximis et Minimis* (also known as the *Nova Method of Greatest and Least*). Newton concluded that Leibniz may have obtained his notes from him and presented them to the Royal Society. Discontent among European mathematicians and English-speaking mathematicians about the contributions of foreign mathematicians became evident. The non-English-speaking mathematicians are now having a fair amount of difficulty dealing with this type of animosity. Leibniz also developed the present field of study. The new calculus he termed "differential calculus" is heavily influenced by many mathematicians, most of whom are completely unknown to the general public. In 1748, Maria Gaetana Agnesi produced the earliest and most thorough treatise on estimating, which has since remained the definitive work.

This equation deals with the evolution of axioms and definitions, and hence its genesis pertains to the advancement of both. During the early years of calculus, two major writers both opposed it. The first was French priest and mathematician Michel Rolle,

and the second was American bishop and philosopher George Berkeley. Berkeley wrote out the infinitesimals as hypothetical subsets of a finite amount, describing a preexisting and finite quantity. Mathematics has developed some of the best experiments up to this day, and that's what calculus is all about, in the 2000's.

An attempt by various mathematicians such as Maclaurin was made to show the validity of arithmetic by using infinitesimals, but this didn't occur until over 150 years later when, due to the efforts of Cauchy and Weierstrass, it was proven that there was a method to avoid arbitrary concepts of small numbers. Weierstrass adopted a basic (generalised) approach that placed emphasis on the notion of continuity and was generally non-inclusive of infinitesimals (although his definition can actually validate nilsquare infinitesimals). The terms limits and infinitesimal calculus are both now used to describe what would now be called "infinitesimal calculus," although limits are still preferred. He derived the notion of the integral by using the ideas of Bernhard Riemann. Over the years, the equations of the equation were applied to the traditional space of the Euclidean (Euclidean space) and the complex plane (complex plane).

Approximation theorems are established using calculus in the context of actual analysis, including the demonstration of approximation theorems. The use of calculus has been observed in a wide number of domains. In the opinion of Henri Lebesgue, however, measurement theory should apply to all save the most diseased functions.

Schwartz presented distributions which are used in the process of finding derivatives of such variables.

Limits is not the most academically formal approach to learn calculus. Abraham Robinson's technique of study is unique, making it a "non-standard" way of doing things. the Robinson system, founded in the 1960s, incorporates numerous arithmetic machines in order to compliment the real number structure, which also includes infinitesimal and infinite numbers. The numbers that come from these computations are known as "hyperreal numbers," which enable Leibniz-like computational rules to be developed. This "additional permission" given to current science not only allows the use of differing power series, but also allows the use of infinitesimals that have been neglected in favour of contemporary science.

## PROPER USE OF CALCULUS

This is one of several facts which underscore that calculus, developed in Greece, China, India, Iraq, Persia, and Japan, started in Europe in the 17th century as a consequence of the work of Isaac Newton and Gottfried Wilhelm Leibniz. Before the notions of instantaneous motion and the existence of fields with curves, calculus was built on previous conceptions such as instantaneous motion and the "field under curves."

Calculus was used to directly contribute to the transfer of technology. The most significant characteristic Equations that involve velocity and inertia, gradient slope, and optimization are all aspects of the application of the calculus. measures such as area, volume, arc length, centre of mass, feature, and strain may all be found in calculus The Fourier series is mostly employed by sophisticated applications.

The method of calculus is utilised to give a more exact explanation of space, time, and motion.

A myriad of mathematicians and scientists have to grapple with the concept of zero spacing and an unlimited number of numbers. These problems are concerned with the motion and the ground. Like many ancient Greek philosophers, Zeno of Elea utilised paradoxes that are being spoken about today.

The use of calculus to resolve paradoxes is described in this passage.

It is generally the case that calculus is developed with relatively tiny numbers. The first way to do so was by using infinitesimals. They are used as numerical values except for the fact that they are "infinitely tiny" in any sense. In other words, when infinity runs out, we'll be faced with the question of whether infinite still exists.

This represents the genuine negative number. The field of Calculus is made up of techniques for the manipulation of infinitesimals. The first two variables on the left side,  $dx$   $dx$  and  $dy$ , were thought to be infinitesimal, and the derivative  $dx/dy$  was the ratio of those two terms. Since it is a simple action to conduct, it may be done at any point throughout the process. For college students, there are plenty of easy things to get into if they take advanced electives outside of mathematics.

Students who are in either algebra or pre-calculus often have difficulties finding coursework that utilises their math. Nevertheless, it was possible for students to accomplish the Calculus Anywhere work since they were not required to comprehend the mathematics (calculus) in their assigned study materials.

They sought to expand calculus to another subject and provide a summary of its applications. For students who have completed a more basic level of mathematics, it may be helpful to have teachers utilise real research articles for their lessons. Instead of having students give out papers, assign students to browse or subscribe to higher-level or undergraduate periodicals. A simpler approach is to advise students to seek for news stories or other sources of information instead of research reports. Another positive effect of having more in-class tasks, rather than homework assignments, is that it allows teachers to keep classroom activities at the right developmental level.

We offer a first approximation of the current status of the calculus field in the introduction of this work, highlighting both the promise of recent research achievements as well as the need for new ideas. At this point, students have a conceptual understanding of the different elements of calculus therefore we begin the process of calculus instruction with a focus on the student's learning comprehension. In middle school, we give pupils laboratory examinations that they must pass in order to have a better knowledge of calculus. At high school, we've conducted the most up-to-date assessment of how well instructors know about the goals and values of their schools and students. Although these patterns tend to occur when people are engaged in educational or learning processes, the phenomenon is really attributed to the existence of a continuum of both learning and teaching on which an individual's level of advancement is situated. Taking into consideration all of the research and developments in the various sections, I see the model of the time of research and development as an appropriate illustration of the primary contributions of the articles. It looks as if our present models are unable to fully explain these gaps, and it is possible that future research will be able to fill in the gaps.

Today, infinite approaches have gone out of favour due to the fact that they have become too abstract to be formally specified. The infinitesimals theory was resurrected in the 20th century, when the development of non-standard analysis and smooth infinitesimal analysis helped rejuvenated it.

A much-used restriction in delta expansion was superseded during the latter part of the 19th century by the replacement of epsilon. When the input increases, the feature will approach but not quite reach the value of the input. This particular section of the theory use the actual number form. The goal of calculus is to govern these thresholds in a predictable manner. The important thing about ideals is that they are often, albeit only rarely, accompanied by smaller amounts, and infinitesimals are considered important in identifying a smaller or lower number. A more rigorous basis for estimates was established as a result, and this is what is considered the standard method to estimate in the twentieth century.

#### **CALCULUS AS A SUBJECT OR A CURIOSITY DOMAIN IN MATHEMATICS-THE BEGINNING OF LOGICAL ERA**

To conclude, calculus purchased a logical interest in mathematics for researchers, scientists, students, and for many others, which helped to the development of many of the contemporary technologies and their fundamentals which are now crucial parts of everyone's life.

In addition to the formulas mentioned above, applications of physics, chemistry, and biology are well-known and may have occasional importance in calculus teaching. Calculus may be applied in a variety of fields of study. It is noted by AMATYC that students will engage in mathematics topics of interest to them and this serves to increase their understanding of the field (AMATYC, 2006, p. 10). Calculus may be employed in a very limited number of sectors in which the vast majority of pupils show little interest in pursuing a profession. As a result, academics are expected to facilitate students' understanding of the relevance of mathematics in their chosen professional path.

Many studies say that in mathematics there has been a significant reduction in the general efficiency of pupils from grade nine to grade twelve. Despite this, it is possible that this is caused by pupils being required to go through extreme examples of arithmetic homework (Duan, Depaepe, & Verschaffel, 2011). When dealing with a more sophisticated or convoluted problem, more sophisticated approaches are needed and the processing requirements will be considerable.

In order to make students aware of mathematics' capacity to solve issues that are important to them, but without devoting excessive class time to mathematics, this article gives them a sense of what mathematics may do. To assist students of all ages to better understand mathematics, this system is designed to increase students' understanding (AMATYC, 2006). Additionally, the aim is to inspire women who are interested in mathematics and who want to advance in their careers.

More often than not, researchers have found that women desire to interact and have discovered that social expectations are involved in the choice of a vocation.

## **THE IMPLEMENTATION OF THE DIRECTIVE**

Calculus Everywhere is made up of two distinct concepts. Following this introduction, students learn how mathematics is used in a variety of disciplines. There are several references in which examples are drawn from the research papers to assist students link the equations they learn in class to an array of subjects of societal significance. In this case, the presentation is used to address the mathematics that were employed in the report. Also, we're inquiring about the many academic areas and careers that might be used in pursuit of academic degrees.

In a session for new students at one of our institutions, students have identified many reasons pertinent to their respective majors. In the forensics and criminology major realm, a well-rounded selection of enlightening but proficient books has been assembled to keep students of all levels intrigued. We selected the estimate implementation options.

These researchers emphasised the serious social concerns facing Africa (Sachs, McArthur, Schmidt-Traub, & Kruk, 2004), but they were precise in their focus on a major social concern. Applying for an absentee ballot in the recent 2012 presidential election was incredibly easy since applications were processed quickly.

The assignment has two components, which are a homework assignment and a personal project. First, students are supposed to go to the Internet to find a research paper that the equation has been applied to.

They most certainly have this job for the long haul. In order to put up a well-informed essay, students must first investigate a certain issue and then compose a one-and-a-half-page overview of the scenario, covering the facts of arithmetic and the issue of function.

## **THE POSSIBLE STUDENT CHALLENGES ARE**

When preparing for an in-class task, we require students to apply an article and a one-sentence summary of mathematics. Students who have the luxury of doing their work without the interruption of others appreciate this benefit. By the end of the first fifth of it.

A few of pupils failed to identify an acceptable article on their first attempt, and the teacher's recommendations were quite helpful to these students when it came to locating an appropriate article.

Even when barriers, such as student-generated review papers, blog entries, and instructor-created workbooks, have stood in their way, certain students have proven to be tough to identify.

Since I needed to find many source books for my research, this project was well-suited for my needs. It was difficult for our calculus I students since, having had zero prior exposure of our library, they were undergraduate students at the time. More relevant literature research has been initiated and students will be led to relevant searches or original sources. Many of our students had to choose worthwhile papers, as well as provide insightful descriptions of various mathematical applications.

### **The responses of the students**

To raise our students' knowledge of the significance of mathematics in society, we have been trying to strengthen the students' understanding of this idea. The data which reveals this student's feeling about mathematics, as well as their choices in taking mathematics classes that lead to social problems, originates from studies which indicate how they feel about the subject, how much they value it in the world, and what their choices are when it comes to choosing math classes. The replies given are an example of a prevalent pattern among students.

## **PAYING ATTENTION TO THE SUBJECT**

For the most part, the majority of students in their essays on the social relevance of mathematics have exhibited a significant growth in their understanding of this value. Once the two students realised how important calculus was for them, their perspectives changed from thinking that calculus was not very valuable for their futures to thinking that it was a critical part of their future success. Following the reading of this essay,

This student had the desire of becoming a doctor, and he felt that an MRI was impossible without a calculus, and that physicians had to learn calculus to be able to work in the field.

To ensure consistent dosing for all patients, various drugs are administered to patients at varied steady-state dosages.

The pupils have shown an interest in social subjects. The student decided to focus on an article that dealt with a simple way to quantify the concentration of illegal substances. A publication published in one prominent geography journal said that researchers are using a spatial paradigm in order to better understand how people carry out their activities in various locations. The model is useful for persons participating in social studies since it offers an overview of the impacts that possible conclusions have on citizens' lives and economic progress, whether those people are researching locations in the global south, the global north, or throughout the globe.

Data for this report was compiled from two separate sources: student participation in the Calculus Anywhere activity, as well as survey data collected from students and faculty immediately before and after the semester in which the activity was performed. The ATMI survey features a self-confidence survey, if you will.

Algebra is fun and motivating. Since it has been shown to be useful in learning arithmetic, we've directed students' replies to math. Despite this, the large majority of students (or the plurality of students) chose not to take mathematics (studies) because they did not feel it would be effective to address everyday difficulties. However, for the majority of pupils, mathematics did not seem to be relevant in their daily lives. Students have almost no expectations of using math in their personal or professional lives.

Academic life all through the first year of school. This means that since we queried our students, the findings indicate that numerous pupils dislike mathematics and don't believe it is practical. It was noted that with each lesson learned, the majority of pupils responded positively to all three concepts.

## CONCLUSION

The impact of this expansion was seen throughout many semesters from its introduction. In the first semester, we made it clear to students that they were not required to write a literature review; they were just to draught one.

At the beginning of the first semester, we noticed that we needed to add more information about the exercise, and we also wanted to talk to students beforehand about their opinions on the operation before the third semester in order to get a better grasp of their opinions. For grading reasons, we'll suggest that you complete these tasks so that you get two times the normal credit. Students would feel more motivated to be a part of the goal if they were aware of their mean test result. Regardless of the two subjects we are going to discuss, we will also give our pupils with a simple and clear header that explains what kinds of themes are on their minds in an essay.

As well as how the explanation may have been graded. Instructions have been revised to enable students to write on how this application may be applied in a sector of work.

## REFERENCES

1. Arnon, I., Cottrill, J., Dubinsky, E., Oktac, A., Fuentes, S., Trigueros, M., et al. (2014). *APOS theory: A framework for research and curriculum development in mathematics education*. New York, NY: Springer.
2. Artigue, M. (1994). Didactical engineering as a framework for the conception of teaching products. In R. Biehler, R. W. Scholz, R. Sträßer, & B. Winkelmann (Eds.), *Didactics of mathematics as a scientific discipline* (pp. 27–39). Dordrecht, The Netherlands: Kluwer Academic Publishers
3. Artigue, M., & Mariotti, M. A. (2014). Networking theoretical frames: the ReMath enterprise. *Educational Studies in Mathematics*, 85, 329–355.
4. Asiala, M., Cottrill, J., Dubinsky, E., & Schwingendorf, K. E. (1997). Networking theoretical frames: the development of students' graphical understanding of the derivative. *The Journal of Mathematical Behavior*, 16(4), 399–431.
5. Aspinwall, L., Shaw, K. L., & Presmeg, N. C. (1997). Uncontrollable mental imagery: graphical connections between a function and its derivative. *Educational Studies in Mathematics*, 33(3), 301–317.
6. Baldino, R. R., & Cabral, T. C. B. (1994). Os quatrodiscursos de Lacan eo Teorema Fundamental do Cálculo. *Revista Quadrante*, pp. 1–24.
7. Barbosa, S.M. (2009). *Tecnologias da Informação e Comunicação, Função Composta e Regra da Cadeia*. Doctoral Dissertation, UNESP, Rio Claro, Brazil.
8. Bergé, A. (2008). The completeness property of the set of real numbers in the transition from calculus to analysis. *Educational Studies in Mathematics*, 67, 217–235.
9. Bikner-Ahsbals, A., & Prediger, S. (2014) (Eds.), *Networking of theories as a research practice*. New York, NY: Springer.
10. Borba, M. C., & Villarreal, M. E. (2005). *Humans-with-media and the reorganization of mathematical thinking: Information and communication technologies, modeling, experimentation and visualization*. New York, NY: Springer.
11. Britton, S., & Henderson, J. (2013) *Issues and trends: a review of Delta conference papers from 1997 to 2011*. Lighthouse Delta 2013: The 9th Delta Conference on teaching and learning of undergraduate mathematics and statistics, pp. 50–58.

12. Chevallard, Y. (1999). L'analyse des pratiques enseignantes en théorie anthropologique du didactique. *Recherches en Didactique des Mathématiques*, 19(2), 221–266.
13. Christensen, W. M., & Thompson, J. R. (2012). Investigating graphical representations of slope and derivative without a physics context. *Physical Review Special Topics-Physics Education Research*, 8(2).
14. <http://journals.aps.org/prstper/abstract/10.1103/PhysRevSTPER.8.023101>.
15. Cobb, P. (1992). A constructivist alternative to the representational view of mind in mathematics education. *Journal for Research in Mathematics Education*, 23(1), 2–33.
16. Cobb, P., Confrey, J., diSessa, A., Lehrer, R., & Schaubel, L. (2006). Design experiments in educational research. *Educational Researcher*, 32(1), 99–113.
17. Code, W., Piccolo, C., Kohler, D., & MacLean, M. (2014, this issue). Teaching methods comparison in a large calculus class. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0582-2.
18. Davis, R. B., & Vinner, S. (1986). The notion of limit: some seemingly unavoidable misconception stages. *Journal of Mathematical Behavior*, 5(3), 281–303.
19. diSessa, A. A. (1988). Knowledge in pieces. In G. Forman & P. Pufall (Eds.), *Constructivism in the computer age* (pp. 49–70). Hillsdale, NJ: Lawrence Erlbaum Associates.
20. Dullius, M. M., Araujo, I. S., & Veit, E. A. (2011). Ensino e Aprendizagem de Equações Diferenciais com Abordagem Gráfica, Numérica e Analítica: um experiência em Cursos de Engenharia. *Bolema. Boletim de Educação Matemática (UNESP. Rio Claro. Impreso)*, Vol. 24, pp. 17–42.
21. Eichler, A., & Erens, R. (2014, this issue). Teachers' beliefs toward teaching calculus. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0606-y.
22. Ellis, J., Kelton, M. L., & Rasmussen, C. (2014, this issue). Student perceptions of pedagogy and associated persistence in calculus. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0577-z.
23. Ferrini-Mundy, J., & Graham, K. (1991). An overview of the calculus curriculum reform effort: issues for learning, teaching, and curriculum development. *American Mathematical Monthly*, 98(7), 627–635.
24. Furinghetti, F., & Paola, D. (1988). Wrong beliefs and misunderstandings about basic concepts of calculus (age 16–19). In *Proceedings of the 39<sup>th</sup> rencontre Internationale de la CIEAEM, 1987* (pp. 173–177). Sherbrooke, Canada.
25. Gravemeijer, K. (1994). *Developing realistic mathematics education*. Utrecht, The Netherlands: CD Press.
26. Gray, E., & Tall, D. (1994). Duality, ambiguity, and flexibility: a “proceptual” view of simple arithmetic. *Journal for Research in Mathematics Education*, 25(2), 116–140.
27. Häikiöniemi, M. (2004). Perceptual and symbolic representations as a starting point of the acquisition of the derivative. In Hoines, M. J. & Fuglestad, A. B. (Eds.), *Proceedings of the 28th Annual Meeting of the International Group for the Psychology of Mathematics Education*, Vol. 3, pp. 73–80.
28. Hannula, M. S. (2012). Exploring new dimensions of mathematics-related affect: embodied and social theories. *Research in Mathematics Education*, 14(2), 137–161.
29. Hershkowitz, R., Schwarz, B. B., & Dreyfus, T. (2001). Abstraction in context: epistemic actions. *Journal for Research in Mathematics Education*, 32, 195–222.
30. Hershkowitz, R., Tabach, M., Rasmussen, C., & Dreyfus, T. (2014). Knowledge shifts in a probability class: a case study. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0576-0.
31. Javaroni, S. (2007). *Abordagem geométrica: possibilidades para o ensino e aprendizagem de Introdução às Equações Diferenciais Ordinárias*, Doctoral Dissertation. Rio Claro, Brazil: UNESP.
32. Job, P., & Schneider, M. (2014, this issue). Empirical positivism, an epistemological obstacle in the learning of calculus. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0604-0.
33. Kabael, T. (2010). Cognitive development of applying the chain rule through three worlds of mathematics. *Australian Senior Mathematics Journal*, 24(2), 14–28.
34. Rasmussen, C., Wawro, M., & Zandieh, M. (2012). Four lenses for examining individual and collective level mathematical progress. Paper presented at the annual meeting of the American Educational Research Association, Vancouver, Canada.
35. Salinas, P. (2013). Approaching calculus with SimCalc: linking derivative and antiderivative. In S. J. Hegedus & J. Roschelle (Eds.), *The SimCalc vision and contributions* (pp. 383–399). Dordrecht, The Netherlands: Springer.
36. Schoenfeld, A. (1994). Some notes on the enterprise (research in collegiate mathematics education, that is). *Research in Collegiate Mathematics Education*, 1, 1–19.
37. Sealey, V. (2014). A framework for characterizing student understanding of Riemann sums and definite integrals. *The Journal of Mathematical Behavior*, 33, 230–245.
38. Sfard, A. (1991a). On the dual nature of mathematical conceptions: reflections on processes and objects as different sides of the same coin. *Educational Studies in Mathematics*, 22, 1–36.
39. Sfard, A. (1991b). On the dual nature of mathematical conceptions: reflections on processes and objects as different sides of the same coin. *Educational Studies in Mathematics*, 22(1), 1–36.

40. Shadish, W. R., Cook, T. D., & Campbell, D. T. (2001). *Experimental and quasi-experimental designs for generalized causal inference*. Boston: Houghton Mifflin.
41. Soares, D. S. (2012). *Uma abordagem pedagógica baseada na análise de modelos para alunos de biologia: qual o papel do software?* Doctoral Dissertation, UNESP, Brazil.
42. Soares, D. S., & Borba, M. (2014, this issue). The role of software Modellus in a teaching approach based on model analysis. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-013-0568-5.
43. Swidan, O., & Yerushalmy, M. (2014, this issue). Learning the indefinite integral in a dynamic and interactive technological environment. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0583-1.
44. Tall, D., & Vinner, S. (1981). Concept image and concept definition in mathematics with particular reference to limits and continuity. *Educational Studies in Mathematics*, 12(2), 151–169.
45. Thompson, P. W. (1992). Notations, conventions, and constraints: contributions to effective uses of concrete materials in elementary mathematics. *Journal for Research in Mathematics Education*, 23, 123–147.
47. Thompson, P. W., & Silverman, J. (2008). The concept of accumulation in calculus. In M. Carlson & C. Rasmussen (Eds.), *Making the connection: Research and teaching in undergraduate mathematics* (pp. 117–131). Washington, DC: The Mathematical Association of America.
48. Tinto, V. (2004). Linking learning and leaving. In J. M. Braxton (Ed.), *Reworking the student departure puzzle*. Nashville, TN: Vanderbilt University Press.
49. Törner, G., Potari, D., & Zachariades, T. (2014, this issue). Calculus in European classrooms: curriculum and teaching in different educational and cultural contexts. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0612-0.
50. Trigueros, M., & Martínez-Planell, R. (2010). Geometrical representations in the learning of two-variable functions. *Educational Studies in Mathematics*, 73(1), 3–19.
51. Weigand, H.-G. (2014, this issue). A discrete approach to the concept of derivative. *ZDM—The International Journal on Mathematics Education*. doi:10.1007/s11858-014-0595-x.